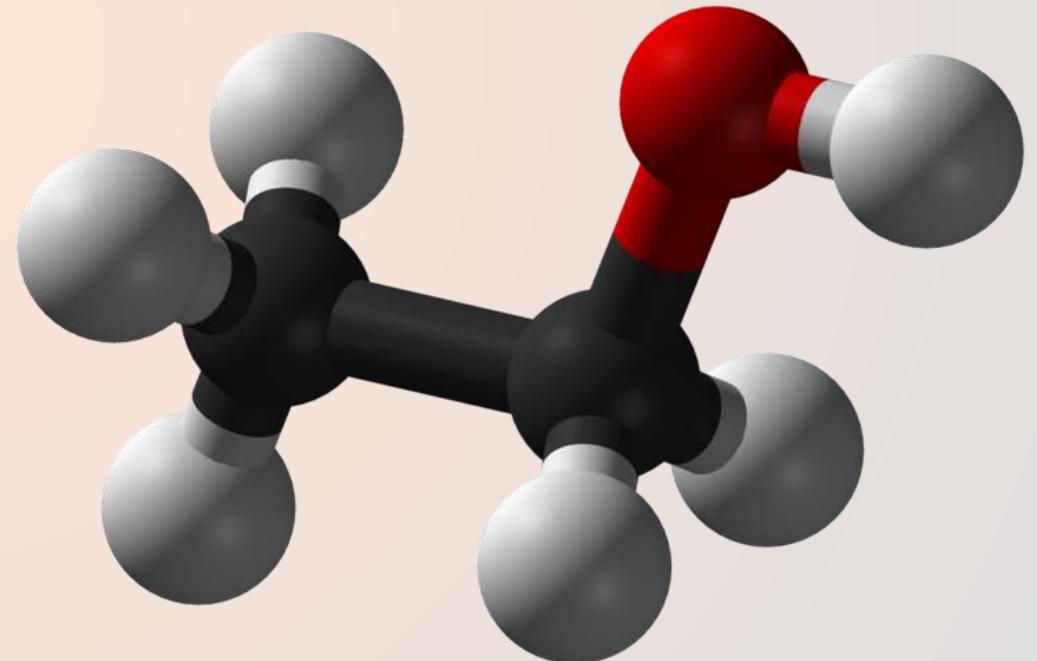


# Molecular spectroscopy for exoplanets

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*& Isabelle Kleiner (Laboratoire interuniversitaire  
des systèmes atmosphériques, Créteil)*

*+ see credits at the end*



INFRARED AND RAMAN SPECTRA  
of  
POLYATOMIC MOLECULES

BY

GERHARD HERZBERG, F.R.S.C.  
*Research Professor of Physics,  
University of Saskatchewan*

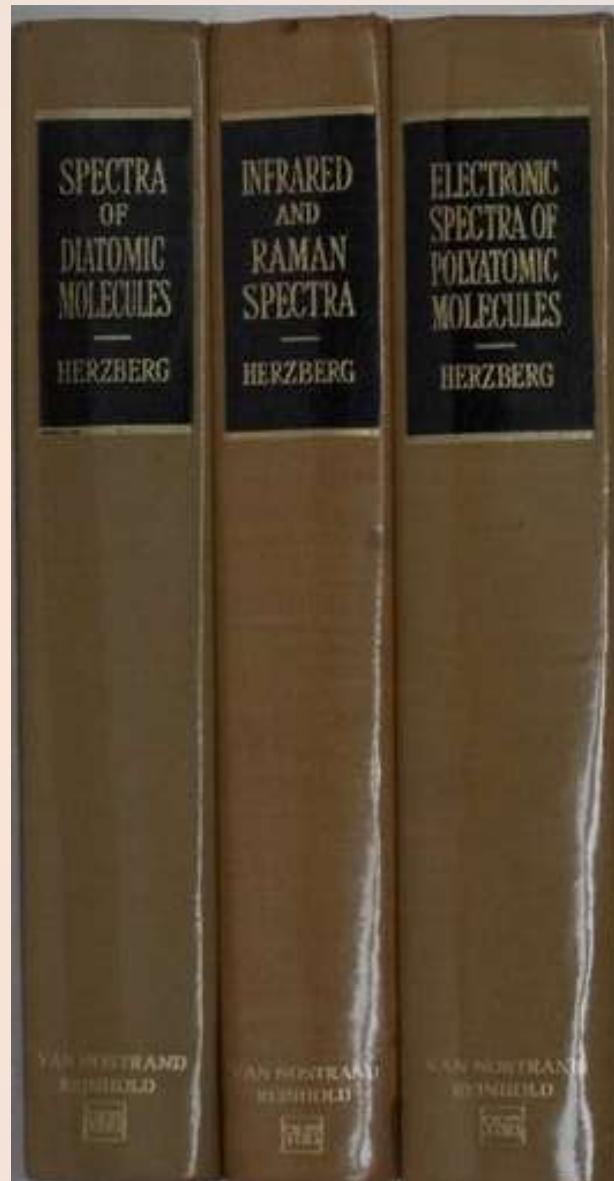
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*Forming the second volume of  
MOLECULAR SPECTRA AND  
MOLECULAR STRUCTURE*

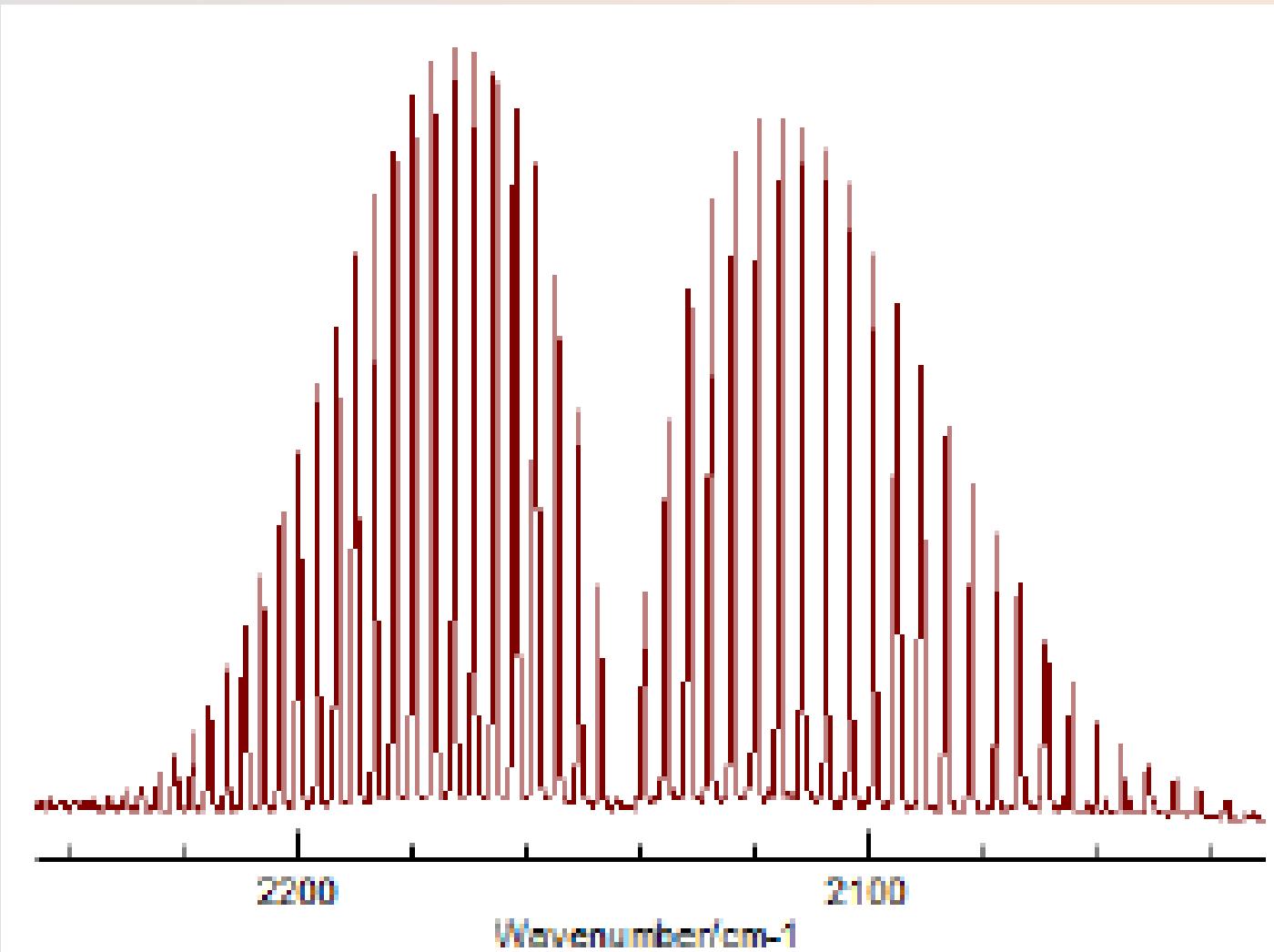
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# What is spectroscopy ?



*CO vibration – rotation band at 4.3 micrpn*



# The Born-Oppenheimer approximation

**Problem** : solve the Heisenberg equation for a molecule :  $H \Psi(q_i, Q_i) = E \Psi(q_i, Q_i)$   
↔ Find the eigenvalues E of the Hamiltonian operator H

*Heisenberg, W. (1925) Über quantentheoretische Umdeutung kinematischer und mechanischer Beziehungen. Zeitschrift für Physik, 33, 879-893.*

Due to the large differences in masses of the nuclei and of the electrons, the Born-Oppenheimer approximation stipulates that the electronic part of the wave function can be decoupled from the nucleus part with  $q_i$  the electronic and  $Q_i$  the nuclear coordinates

$$\Psi(q_i, Q_i) = \Psi_{el}(q_i; Q_i) \Psi_N(Q_i)$$

The total energy of the molecule is the sum of :

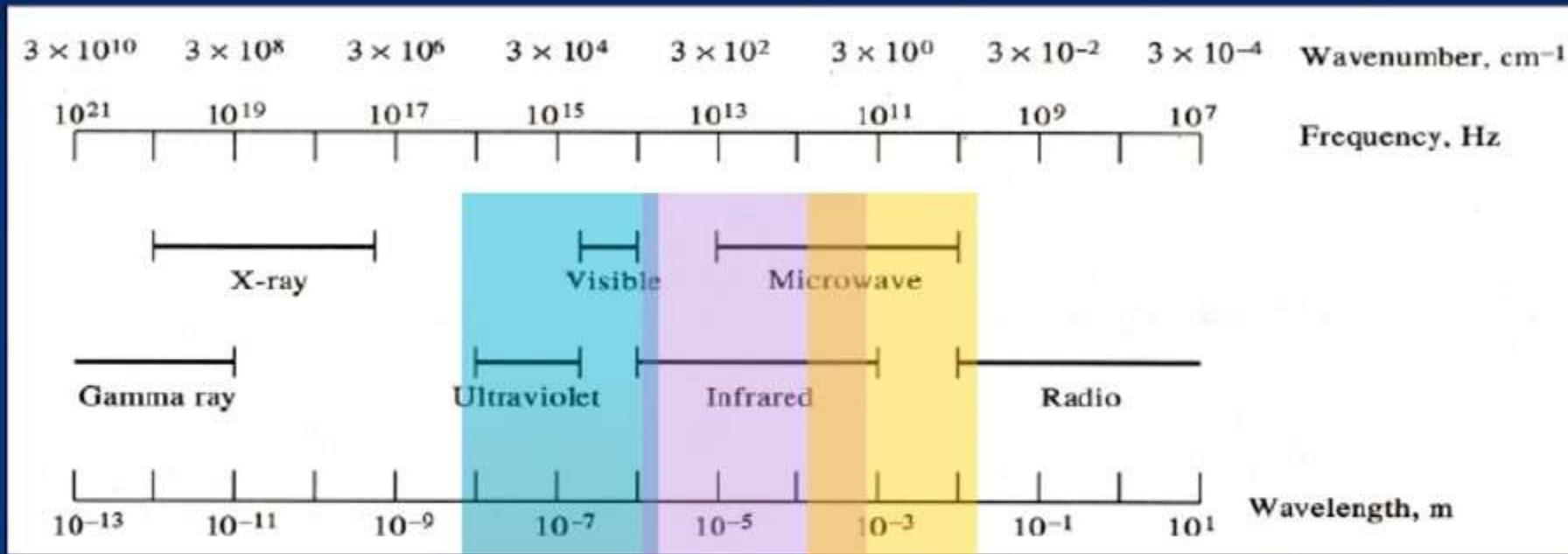
- An electronic part
- A vibrational part
- A rotational part

which can be solved independently

*Max Born; J. Robert Oppenheimer (1927). "Zur Quantentheorie der Moleküle". Annalen der Physik. 389 (20): 457–484.*



# Spectral range and molecular motions



# Electronic structure

Recipe: freeze the nuclei at fixed position and solve the electronic Schrödinger equation :

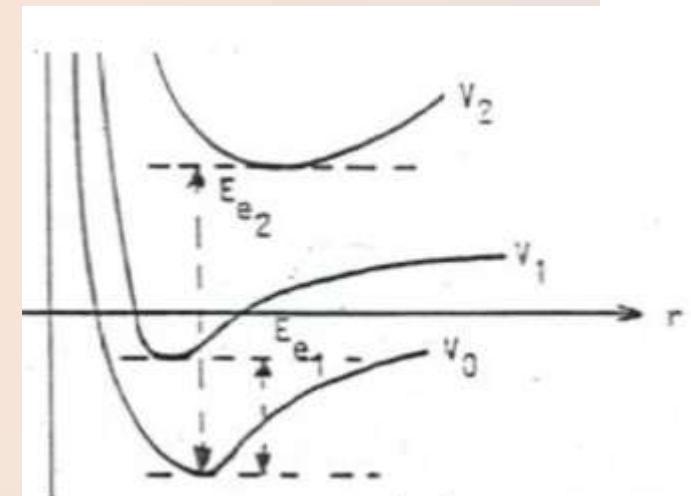
$$H_{el} \Psi_{el} = E_{el} \Psi_{el}$$

Where

$$H_{el} = T_e + V_{ne} + V_{ee}$$

is the potential energy of the electrons. The Term associated to the electric repulsion of the nuclei is simply an additional constant  $V_{nn}$ .

Example for a diatomic molecules



# Lines, bands, systems : the components of spectra

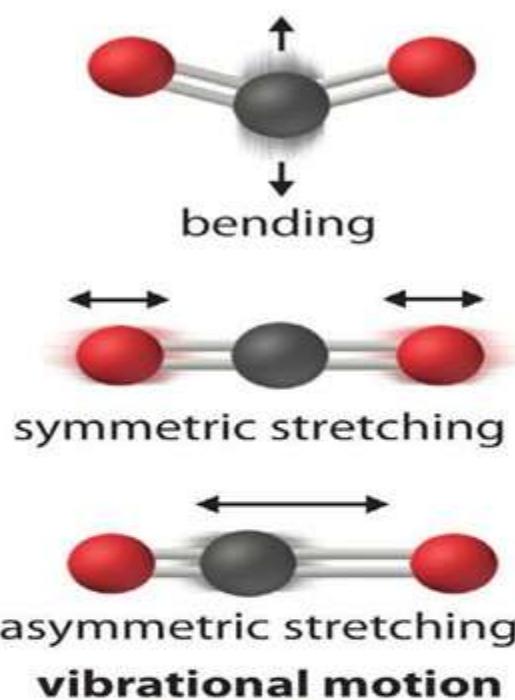
See

- Hanson, Summer School on Combustion and the Environment, June 19-24, 2022, Princeton, NJ, USA

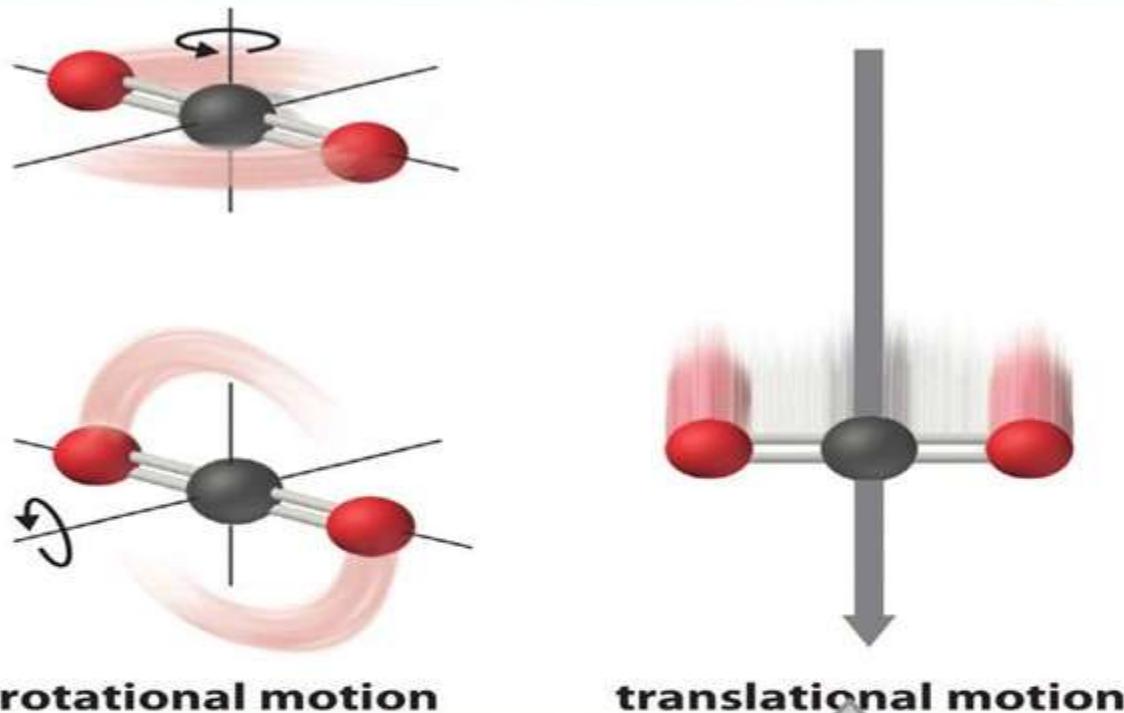
<https://cefrc.princeton.edu/sites/g/files/toruqf1071/files/documents/Lecture%20Notes%20-%20Hanson.pdf>



## 3 types of nuclear motions



**Harmonic  
Oscillator  
model**



**Rigid rotor  
model**

Can be separated  
From the other motions  
Energy = constante

# Rigid rotor model of diatomic molecule

## Vibration of diatomic molecules

## Classification of polyatomic molecules

## The rotation of polyatomic molecules

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<https://cefrc.princeton.edu/sites/g/files/toruqf1071/files/documents/Lecture%20Notes%20-%20Hanson.pdf>



## Rotational constants are related to molecular structure

For diatomics we defined a rotational constant  $\tilde{B} \propto \frac{1}{I} = \frac{1}{\mu R^2}$

In general we require three such rotational constants:

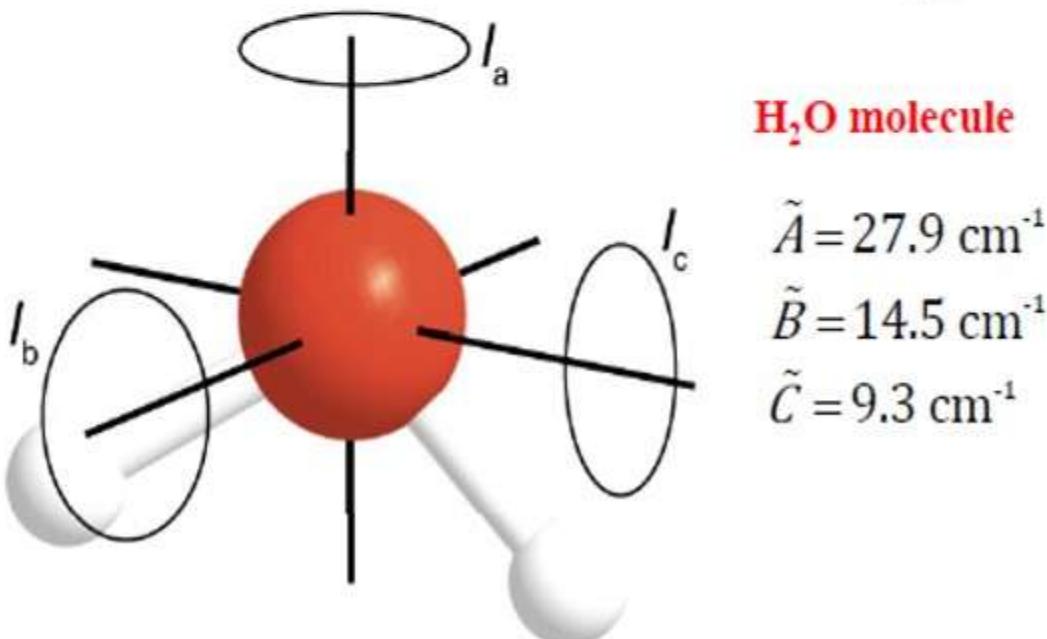
as wavenumbers:

$$\tilde{A} = \frac{h}{8\pi^2 c I_a}$$

$$\tilde{B} = \frac{h}{8\pi^2 c I_b}$$

$$\tilde{C} = \frac{h}{8\pi^2 c I_c}$$

$$\tilde{A} \geq \tilde{B} \geq \tilde{C}$$



But, we can no longer relate these constants explicitly to individual bond lengths within the molecule.

# Symmetries

- Symmetry elements and operations
  - Plane of symmetry ( $\sigma$ )
  - Center of symmetry (i)
  - P-fold axis of symmetry  $C_p$  with  $p=1,2,3\dots$
  - P-fold rotation-reflection axis  $S_p$  (rotation  $C_p$  + symmetry)
- Point groups

The combination of the symmetry elements (+ identity) forms a group structure and characterize the molecular structure relevant to the vibrational fundamentals

# Concept of normal vibrations - fundamentals

## Types of bands

See

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<https://cefrc.princeton.edu/sites/g/files/toruqf1071/files/documents/Lecture%20Notes%20-%20Hanson.pdf>



# Additional complexities : internal motions

Molecules with internal motions have additional complexity in their spectroscopy

Examples :

- $\text{NH}_3$  : inversion motion
- $\text{CH}_3\text{-OH}$  : methanol
- $\text{CH}_3\text{-SH}$  : methylmercaptan
- $\text{CH}_3\text{-C=OH}$  : acetaldehyde

